# **Heuristic Method for Evaluating Coil Performance**

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A heuristic methodology is described that was developed to evaluate the chemical efficiency of high-power chemical oxygen iodine laser (COIL) devices and its application to the specific evaluation of the U.S. Air Force Phillips Laboratory's RotoCOIL laser. A heuristic equation that forms the basis of this methodology and describes the COIL energy flow, energy losses, and power extraction using measured data, code results, and empirical relations is presented. Using this equation and bounding values for some of its terms, it is shown that for the RotoCOIL performance data the experimentally measured average  $O_2(^1\Delta)$  yield of 0.40 is nearly 38% below that which would be consistent with the measured extraction power. By relating terms of the heuristic equation to performance of individual components of the COIL system, it is concluded that nearly 50% of the efficiency loss for the RotoCOIL laser derives from oxygen generator and delivery losses, whereas 15% is from nozzle inefficiencies and 11% from resonator losses.

	Nomenclature	$R_{\rm out}, R_{\rm max}$	= mirror reflectivities for resonator output and
$\boldsymbol{A}$	= cross-sectional flow area in the optical cavity		maximum reflectivity mirrors
$A_{\text{out}}, A_{\text{max}}$	= mode footprint area at outcoupler and maximum reflectivity mirrors	$S_{ m out},S_{ m max}$	<ul> <li>mirror scattering losses for resonator output and maximum reflectivity mirrors</li> </ul>
$\dot{\mathrm{Cl}}_2$	= chlorine flow rate into generator, mole/s	$T_{ m cav}$	= static cavity gas temperature
F	= iodine dissociation fraction	$T_{ m cavo}$	= static cavity gas temperature with no dissociation
$G_o$	= average small signal gain in direction of optical	$U_{\mathrm{Cl}_2}$	= chlorine utilization defined by Eq. (3)
V	axis	v	= average flow velocity
$G_{th}$	= threshold gain	$x_{\rm ef}$	= $e$ -folding length for the reduction of $O_2(^1\Delta)$ during power extraction
$I_2$	= iodine flow rate	Y	= singlet delta oxygen yield defined by Eq. (4)
$K_{\rm deact}$	= rate coefficient for quenching of I* by H <sub>2</sub> O	$Y_{\rm cav}$	= singlet delta yield in cavity
$K_g$	= defined by Eq. (15)	$Y_{\text{deact}}$	= singlet delta yield loss as a result of water
$k_{ m eq}$	= equilibrium constant for I atom pumping reaction, Eq. (5)	4 deact	deactivation of I* in laser cavity
$k_F, k_R$	= rate coefficients for I atom pumping reaction, Eq.	$Y_{ m diss}$	= singlet delta yield loss during dissociation
, , , ,	(5), and reverse reaction, Eq. (6)	$Y_{ m plen}$	= singlet delta yield just upstream of the $I_2$ injection
$k_1$	= chlorine utilization rate parameter, defined in	$Y_{\rm th}$	= minimum singlet delta yield for positive gain
·	Ref. 14	$\gamma_w$	= heterogeneous quenching probability of $O_2(^1\Delta)$
$k_3$	= $O_2(^1\Delta)$ production rate parameter, defined in		on basic hydrogen peroxide
5	Ref. 14	$\eta_{ m chem}$	= overall chemical efficiency of laser defined by
$L_{g}$	= gain length		Eq. (1)
$L_m^{\circ}$	= length of the optical extraction mode in the flow	$\eta_{ m ext}$	= optical extraction efficiency
•••	direction, cm	$\eta_{ ext{cxtm}}$	= medium extraction efficiency
N	= number of singlet delta oxygen molecules to	$\eta_{ m extr}$	= resonator extraction efficiency
	dissociate an iodine molecule	$\eta_{ m geo}$	= fraction of flow interrogated by resonator normal
$N_A$	= Avogadro's number		to the flow and optic axis
$P_{\mathrm{av}}$	= power available in cavity	$\eta_{ m mix}$	= accessed $O_2(^{\dagger}\Delta)/total O_2(^{\dagger}\Delta)$
$P_{\mathrm{out}}$	= power extracted from resonator	$\eta_{ m res}$	= flow residence time efficiency
$\mathcal{P}^{\circ}$	= fraction of the outcoupled power lost as a result of	σ	= gain cross section
	diffraction effects	$\phi$	= COIL chemistry parameter defined by Eq. (28)
		91	= lasing energy of 1 mole of I*, kJ
		[]	= species concentration in number per cubic

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# I. Introduction

centimeter

▼ HEMICAL oxygen-iodine laser (COIL) device technology has advanced steadily over the last 10 years. Table 1 shows a partial, chronological listing of reported performance for a number of devices. It is mostly restricted to larger, supersonic devices generating power in the range of kilowatts to tens of kilowatts. It shows a simple overall chemical efficiency  $\eta_{chem}$  defined as

$$\eta_{\text{chem}} = \frac{P_{\text{out}}}{91\dot{\text{Cl}}_2} \tag{1}$$

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Table 1 COIL chemical efficiency performance history

Year	Ref.	Location <sup>a</sup>	Efficiency
1984	1	USA (AFWL)	0.116
1984	2	USA (AFWL)	0.147
1985	3	USA (RD)	0.138
1987	4	USA (AFWL)	0.175
1988	5	USA (AFWL)	0.231
1989	6	USA (AFWL)	0.236
1989	7	USA (RD)	0.209
1995	8	Russia	0.1
1991	9	USA (PL)	0.181
1995	10	Israel	0.05
1993	11	USA (PL)	0.134

<sup>a</sup>AFWL = Air Force Weapons Laboratory, RD = Rockwell International/Rocketdyne, and PL = Phillips Laboratory.

where the outcoupled power  $P_{\rm out}$  is compared with the total device chlorine flow  $\dot{C}l_2$  in mole/second. The factor 91 is the energy, in kilojoules, for one mole of iodine atoms, the lasing species, in the upper level of the lasing transition. This is an overall, end to end, all inclusive assessment parameter, the elements of which will be discussed later. The energy of singlet delta oxygen, 94.4 kJ/mole, is not utilized in this efficiency factor. This 4% loss is inherent in transferring this energy to atomic iodine in the COIL concept (i.e., the pumping reaction is slightly exothermic).

Table 1 shows that the best efficiency for any device of size is 0.24 for RotoCOIL. The obvious question is: where has the energy gone? What happened to 75% of the chemical energy? It is the purpose of this paper to answer this question as well as possible in view of incomplete and sometimes suspect data.

#### II. Heuristic Equation

The heuristic equation to be developed is based upon tracking the energy in a COIL device, starting with the incoming  $\text{Cl}_2$  flow and ending with the outcoupled optical power, accounting for the losses along the way.

#### **Heuristic Equation Development**

Figure 1 shows a schematic of a generalized COIL device. The flow is from left to right. A mixture of chlorine and helium is introduced into an oxygen generator, where it contacts basic hydrogen peroxide (BHP). In the case of the RotoCOIL device, the generator is an assembly of thin disks that rotates into a bath of BHP and then picks up a thin film of liquid as it is rotated out of the BHP into the chlorine/helium flow. The overall reaction that takes place on the film is

$$Cl_2 + 2KO_2H \rightarrow O_2(^1\Delta) + H_2O_2 + 2KCl$$
 (2)

This reaction produces excited oxygen, ground state oxygen, and, because the reaction is not complete, some residual chlorine. Also, because the film surface heats up because of the reaction, some water vapor is produced.

The efficiency of using chlorine is called the utilization  $U_{Cl_2}$ :

$$U_{\text{Cl}_2} = 1 - \frac{\text{residual chlorine}}{\text{total chlorine}}$$
 (3)

The efficiency in generating excited oxygen is called yield Y:

$$Y = \frac{\text{excited oxygen}}{\text{total oxygen}} = \frac{O_2({}^{1}\Delta)}{O_{2 \text{total}}}$$
(4)

Usually the flow then passes through a cold trap, as shown, to reduce the water content. From the cold trap the flow is ducted to the subsonic entrance channel of the nozzle. In RotoCOIL,  $I_2$  is injected as shown in Fig. 2. In subsequent processes the  $I_2$  is dissociated. This uses some of the excited oxygen. From a macroscopic point of view, during dissociation N molecules of excited oxygen have been expended to dissociate one molecule of  $I_2$ . From energy considerations, N must be at least 2. Because some of the excited species participating in the dissociation process are deactivated during the process, N becomes larger than 2. The excited oxygen lost during dissociation is accounted for by  $Y_{\rm diss}$ .

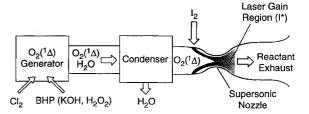


Fig. 1 Supersonic oxygen-iodine chemical laser concept.

The flow is then expanded supersonically into the optical cavity. During the supersonic expansion, energy is transferred to iodine atoms from excited oxygen to provide gain and power. As optical power is coupled out, repumping of the I atoms occurs. This process continues as long as there is gain and as long as the flow is in the optical mode.

Maintenance of positive gain is dependent upon maintaining sufficient excited oxygen. The pumping reaction

$$O_2(^1\Delta) + I \stackrel{k_F}{\to} O_2(^3\Sigma) + I^* \tag{5}$$

is countered by the reverse reaction

$$O_2(^3\Sigma) + I^* \stackrel{k_R}{\to} O_2(^1\Delta) + I \tag{6}$$

The equilibrium constant for these reactions is given by

$$k_{\rm eq}(T) = (k_F/k_R) = 0.75 \exp(401/T_{\rm cav})$$
 (7)

With gain proportional to ([I\*]  $-\frac{1}{2}$ [I]), Eq. (7) leads to the conclusion that there is a minimum amount of excited oxygen required to provide positive gain. This minimum is called the threshold yield  $Y_{th}$  given by

$$Y_{\rm th} = \frac{1}{(1 + 2k_{\rm co})} = \frac{1}{[1 + 1.5 \exp(401/T_{\rm cav})]}$$
(8)

When power extraction reduces the excited oxygen density to  $Y_{th}$ , gain goes to zero and no more power can be extracted. Some of the excited oxygen energy is lost in flowing through the optical cavity as a result of deactivation before the energy is extracted by lasing. One example is the deactivation of  $I^*$  by water vapor after which another excited oxygen repumps the I atom. This reduces the energy pool by one  $O_2(^1\Delta)$  and adds heat to the flow.

When the  $I_2$  is mixed into the primary flow, the process may not provide contact between all of the excited oxygen and the I atoms. A condition where mixing is very poor is shown in Fig. 2. This effect will be accounted for with the parameter  $\eta_{\text{mix}}$ . Because the iodine parameter is the total flow into the device, the density of all iodine species is increased in the mixed region when mixing is poor, e.g., the density of  $I_2$  goes to  $[I_2]/\eta_{\text{mix}}$ .

In experimental laser systems, there is typically an optical aperture placed in the cavity resonator system to define the height and width of the optical mode. This aperture may exclude portions of the flowfield and hence reduce power extraction. This loss is accounted for in the present model by the geometrical efficiency parameter  $\eta_{\rm geo}$ .

Because of losses in optical extraction, such as diffraction, mirror scattering, and absorption, the optical extraction is not 100%. This will be accounted for with an optical extraction efficiency  $\eta_{\text{ext}}$ .

Finally, if power is extracted using a short, in the flow direction, resonator, another efficiency factor  $\eta_{res}$  is required to account for insufficient residence time to deplete the singlet delta oxygen to the minimum level.

Based on the preceding considerations, the heuristic equation for extracted optical power is given by

$$P_{\text{out}} = 91\dot{\text{Cl}}_2 U_{\text{Cl}_2} [Y_{\text{plen}} - Y_{\text{th}} - Y_{\text{diss}} - Y_{\text{deact}}] \eta_{\text{mix}} \eta_{\text{gco}} \eta_{\text{ext}} \eta_{\text{res}}$$
(9)

This equation is not a derived equation. Rather, it is a method of macroscopically accounting for all phenomena in a COIL device that contribute to a reduced chemical efficiency. The Y terms following  $Y_{\text{plcn}}$  represent  $O_2(^1\Delta)$  energy that is not available for optical power extraction, each for different reasons as discussed earlier and later.

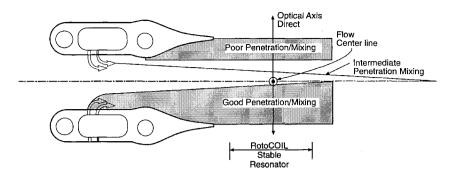


Fig. 2 RotoCOIL supersonic mixing nozzle, the penetration parameter qualitatively describes secondary flow penetration and mixing process in COIL.  $\pi$  = penetration parameter;  $\pi$  =  $(\dot{n}_S/\dot{n}_P)\sqrt{(MW_ST_SP_P/\overline{MW}_PT_PP_S)}$ , where  $\dot{n}$  = molar flow,  $\overline{MW}$  = molecular weight, T = temperature, P = pressure, subscript P = primary flow, and subscript S = secondary injection flow.

In Eq. (9),  $Y_{\text{plen}}$  is introduced because it is customary to try to measure the  $O_2(^1\Delta)$  just upstream of the nozzle. As will be discussed later, there are reaction losses and transport losses as the gas flows through the generator and ducts to the nozzle entrance.

From the preceding description,  $Y_{diss}$  is given by

$$Y_{\rm diss} = \frac{N\dot{\rm I}_2 F}{\dot{\rm C}{\rm I}_2 U_{\rm CI_2} \eta_{\rm mix}} \tag{10}$$

where  $\eta_{\text{mix}}$  appears in the denominator because under poor mixing (Fig. 2), the local  $I_2$  density is on the average larger by this factor.

The term  $Y_{\rm th}$  depends on  $T_{\rm cav}$  as well as the equilibrium rate constant, Eq. (8). When  $\eta_{\rm mix}$  is less than unity, the heat generated during the dissociation process is not distributed throughout the flow. Thus the gas temperature in the mixed zone, where iodine species and therefore the gain reside, is greater than in the fully mixed condition. This is  $T_{\rm cav}$  in Eqs. (7) and (8). Denoting  $\Delta T_{\rm diss}$  as the effect on gas temperature as a result of dissociation and  $T_{\rm cavo}$  as the cavity gas temperature with no dissociation, one can give the effect of the added energy and  $\eta_{\rm mix}$  by

$$T_{\rm cav} = T_{\rm cavo} + \frac{\Delta T_{\rm diss}}{\eta_{\rm mix}} \tag{11}$$
 The term  $Y_{\rm deact}$  can be estimated by integrating the deactivation

The term  $Y_{\text{deact}}$  can be estimated by integrating the deactivation rate over the cavity flow volume. For example, when the primary deactivator is  $H_2O$ , this term would be given by

$$Y_{\text{deact}} = \frac{\int^{V} K_{\text{deact}}[I^*][H_2O] dV}{\dot{C}l_2 U_{\text{Cl}_2} \eta_{\text{mix}}}$$
(12)

where [I $^*$ ] is the actual I $^*$  density during lasing, [H<sub>2</sub>O] is the water vapor density, and this integral is normalized to the oxygen flow to be consistent with the other terms.

Note that  $\eta_{\rm ext}$  is the optical extraction efficiency for the gain medium that is consistent with the physics that gives rise to a particular value of  $\eta_{\rm mix}$ . For a gain medium in which not all of the  $O_2(^1\Delta)$  is accessed by the I containing part of the flow, the average density of I and I<sub>2</sub> species is greater than in the complete, uniformly mixed situation and  $T_{\rm cav}$  is given by Eq. (11).

The flow residence time efficiency  $\eta_{res}$  is given by

$$\eta_{\rm res} = 1 - e^{-L_m/x_{\rm ef}} \tag{13}$$

The *e*-folding distance can be estimated by assuming that the operating gain in the mode is clamped at the threshold gain of the resonator. This assumption that gain is constant and some algebra gives

$$x_{\rm ef} = \frac{Av^2 \eta_{\rm mix}}{2k_F N_A F \dot{\mathbf{I}}_2 K_g} \tag{14}$$

where  $K_g$  is given by

$$K_g = 1 - (I^*/I_t)[1 - (1/k_{eq})]$$
 (15)

With the assumption that gain is clamped to the resonator threshold gain  $G_{th}$ , the ratio of  $I^*$  to the total I atoms  $I_t$  is given by

$$\frac{I^*}{I_t} = \frac{1}{3} \left( 1 + \frac{G_{\text{th}}}{\sigma (293/T_{\text{cav}})^{0.5} F[I_2]} \right)$$
 (16)

Here the iodine number density [I<sub>2</sub>] is given by  $I_2N_A/(Av\eta_{mix})$ .

#### Using the Heuristic Equation

There are many ways the heuristic equation can be used to evaluate COIL data. An example is shown here that will then be applied to RotoCOIL data. The heuristic equation is a collection of parameters, some of which are very well known and some of which are not known at all. The known quantities for a given test data set are  $P_{\text{out}}$ ,  $\dot{\text{Cl}}_2$ ,  $U_{\text{Cl}_2}$ , and  $\dot{\text{I}}_2$ , which are measured test parameters;  $\eta_{\text{geo}}$ , which is determined from the test hardware; and F, which has been measured for certain test conditions. Although  $Y_{\text{plen}}$  was measured during tests, the experimentally determined value has error and, as will be noted later, cannot always be trusted. Thus it will be treated as unknown.

The heuristic equation can be slightly rearranged to

$$\frac{P_{\text{out}}}{91\dot{\text{Cl}}_2} = \eta_{\text{chem}} = U_{\text{Cl}_2}(Y_{\text{plen}} - Y_{\text{diss}} - Y_{\text{th}} - Y_{\text{deact}})\eta_{\text{mix}}\eta_{\text{geo}}\eta_{\text{ext}}\eta_{\text{res}}$$
(17)

This formulation shows all of the contributions to the global chemical efficiency parameter  $\eta_{\rm chem}$  noted earlier.

In this paper, where data from the first seconds of a RotoCOIL test will be evaluated,  $Y_{\text{deact}}$  is very small compared with the other terms and thus will be neglected. Furthermore, for RotoCOIL, at the operating conditions to be evaluated later,  $x_{\text{cf}}$  is about 1.4 cm using the preceding equations. This, plus the geometry of the resonator used in RotoCOIL, gives an estimate of  $\eta_{\text{res}}$  of 0.997. For this paper then,  $\eta_{\text{res}}$  will be assumed to be unity. Rearrangement of Eq. (17), gathering together the known parameters, gives

$$\eta_{\text{mix}}(Y_{\text{plen}} - Y_{\text{th}}) = (K_1/\eta_{\text{ext}} + K_2 N)$$
(18)

where  $K_1$  and  $K_2$  are collections of knowns given by

$$K_1 = \frac{P_{\text{out}}}{91\dot{\text{Cl}}_2 U_{\text{Cl}}, \eta_{\text{geo}}} \tag{19}$$

and

$$K_2 = \frac{\dot{I}_2 F}{\dot{C} l_2 U_{Cl_2}} \tag{20}$$

The  $I_2$  dissociation fraction F is treated as a known for purposes of this paper because it has been measured for conditions in RotoCOIL testing similar to what will be evaluated later.

Equation (18) is then a constraint equation on the unknowns  $Y_{\rm plen}$ , N,  $Y_{\rm th}$ ,  $\eta_{\rm mix}$ , and  $\eta_{\rm ext}$ . Figure 3 shows an example of constraint curves for RotoCOIL-like test conditions for several values of outcoupled power to show the nature of the constraint. These constraint lines do not imply a causal relationship between  $Y_{\rm plen}$  and  $\eta_{\rm mix}$ . Rather, for a measured outcoupled power and for the values of N,  $T_{\rm cav}$ , and  $\eta_{\rm ext}$  assumed for these plots, the unknown parameters  $\eta_{\rm mix}$  and  $Y_{\rm plen}$  are pairwise determined by a point on the constraint line for that power.

The losses shown in the heuristic equation can be gathered together for the major components of a device, namely, the generator, the delivery ducting, the nozzle, and the resonator. For example,  $Y_{\rm plen}$  depends upon generation efficiencies and ducting losses,  $\eta_{\rm mix}$  is associated with the nozzle, and  $\eta_{\rm geo}$  and  $\eta_{\rm ext}$  are associated with

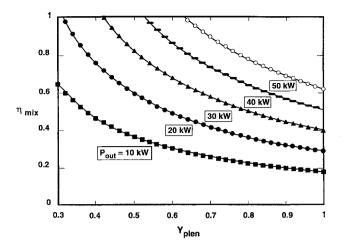


Fig. 3 Effect of  $P_{\rm out}$  on heuristic constraint equation: N=4,  $T_{\rm cav}=150$  K,  $\eta_{\rm ext}=0.8$ , and  $\eta_{\rm geo}=0.9$ .

the resonator. Thus an evaluation of test data with the heuristic equation leads to an evaluation of the major device components. In the following section the heuristic equation will be used to evaluate a particular RotoCOIL test. The parameters N and  $T_{\rm cav}$  will be obtained using an aerokinetics code, and  $\eta_{\rm ext}$  will be determined by resonator properties, gain medium extraction characteristics, and extracted power saturation measurements. An upper limit to  $Y_{\rm plen}$  will be determined using a generator and gas transport code. All of this will be used to determine the limit of parameter space that is consistent with the measured power.

#### III. RotoCOIL Assessment

The highest chemical efficiency for a large COIL device was 0.24 obtained in a RotoCOIL test; see Table 1. The best result to date was obtained in a test carried out Jan. 4, 1990, and designated test 0004HF8. This test has been selected for assessment because it demonstrated the best performance, and this should lead to the least error in partitioning losses.

#### **RotoCOIL Description**

The RotoCOIL device is briefly described next. A more complete description can be found in Ref. 4. The important features to this discussion are indicated next.

The oxygen generator consists of three rotary disk assemblies, the flow of which is combined and then passed through a cold trap to the nozzle. This configuration was selected for expediency, even though this large amount of ducting would be detrimental to performance. The generator/delivery system feeds an array of 42 supersonic nozzle blades where the I2 is injected into the flow in the subsonic region as shown in Fig. 2. This injection upstream of the throat was selected to provide time for mixing and dissociation to take place upstream of the optical cavity. The nozzle array exit dimensions are  $4.4 \times 54.1$  cm. The stable resonator consisted of a spherical mirror of radius 10 m and reflectivity 0.995 and one of several flat outcoupler mirrors having different reflectivities. For test 0004HF8, the outcoupler reflectivity was 0.85. The resonator mirrors were separated 3 m. The width of the optical mode  $L_m$  for this experiment was fixed by upstream and downstream aperture plates at 8 cm, and the vertical dimension of the mode was fixed by the 4-deg diverging cavity side walls. This cavity configuration in conjunction with the symmetric nature of a stable resonator prevented the mode from filling the full cavity flow area giving rise to an  $\eta_{geo}$  of 0.98. The mixing profiles generated by the 42 nozzle blades, including the cores and wakes, are averaged out by aligning the optical axis of the resonator across the nozzle array; see Fig. 2.

# Test 0004HF8 Summary

Table 2 summarizes the pertinent data of test 0004HF8. There are separate data where appropriate for each of the three parallel generators. Except for the  $O_2(^1\Delta)$  measurements, the values for each

Table 2 Operating conditions for test 0004HF8

Parameters	Values
Ċl <sub>2</sub> , mole/s	1.692
He <sub>primary</sub> , mole/s	7.540
He <sub>secondary</sub> , mole/s	2.01
I <sub>2</sub> , mole/s	0.0206
$U_{\text{Cl}_2}{}^{\mathrm{a}}$	0.852, 0.850, 0.851
Y <sub>plen</sub> <sup>a</sup>	0.439, 0.228, 0.530
$T_{\rm plen}^{\rm a}$ , K	304, 321, 327
P <sub>plen</sub> <sup>a</sup> , torr	57.2, 57.2, 57.4
$P_{\rm cav}$ , torr	4.7
$R_{ m out}$	0.85
$\eta_{ m geo}$	0.98
$P_{\rm out}$ , kW <sup>b</sup>	37.2
$\eta_{ m chem}$	0.242

<sup>&</sup>lt;sup>a</sup>Three measurements, one from each of the three generators.

<sup>&</sup>lt;sup>b</sup>Average of 20 and 40 kJ calorimeters.

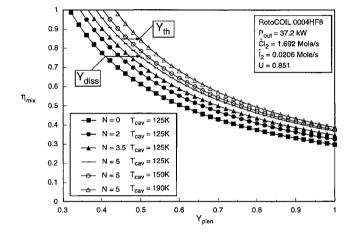


Fig. 4 Effect of N and  $T_{\rm cav}$  on heuristic constraint equation:  $\eta_{\rm ext} = 1.0$  and  $\eta_{\rm geo} = 0.9$ .

generator are very close. This indicates that the generators are operating very nearly the same. In view of this, the wide divergence of the  $O_2(^1\Delta)$  measurements coupled with the failure of initial attempts to reconcile these measurements with the measured power lead to considering  $Y_{\rm plen}$  as an unknown. Based on Table 2, the two constants  $K_1$  and  $K_2$  are 0.2900 and 0.0136, respectively. The term F was taken to be 0.95 based upon actual measurements made on RotoCOIL under very similar flow conditions. These constants give the general constraint conditions for test 0004HF8.

Figure 4 shows a number of constraint lines based upon these constants. The lowest line is with N=0,  $T_{\rm cav}=125$  K, and  $\eta_{\rm ext}=1.0$ . As stated earlier, N must be at least 2 from energy considerations;  $\eta_{\rm ext}$  can be no bigger than 1 by definition. An isentropic flow calculation for this nozzle (area ratio 2) and these flow conditions with no water vapor condensation gives a  $T_{\rm cav}$  of about 125 K. This is the lowest  $T_{\rm cav}$  can be because the flow is not isentropic. Therefore, the lowest curve on Fig. 4 defines the lower bound for  $Y_{\rm plen}$ . The next three lines are N=2, 3.5, and 5 with the other conditions the same. These lines indicate the sensitivity of the constraint line to N. The next two lines are for N=5,  $\eta_{\rm ext}=1$ , and  $T_{\rm cav}=150$  and 190 K, respectively, to indicate the sensitivity of the constraint curve to  $T_{\rm cav}$ .

To provide better estimates for N and  $T_{\rm cav}$  for test 0004HF8, a series of calculations using the one-dimensional RECOIL aerokinetic code<sup>11</sup> were conducted; the results are given in Table 3. The RECOIL model premixes the primary and secondary flows, conserving enthalpy, and calculates the aerokinetic processes from the subsonic region through the throat and into the cavity. The full COIL kinetic rate package of Ref. 12 was used in this calculation. For the premixed model to work, the baseline rate constant of  $7 \times 10^{-15}$  cm³/mol-s for the production of the intermediate species  $I_2^*$  in the iodine dissociation process by  $O_2(^1\Delta) + I_2$  is adjusted by a dissociation rate multiplier of 90-100 to match existing dissociation data. These results show that N is about 4.7 when there is no water

Table 3 One-dimensional RECOIL aerokinetic code calculations for  $T_{\text{cav}}$  and N for test 0004HF8 flow conditions with varying water flow rate (plenum yield = 0.6)

Dissociation rate	Water flow rate, I <sub>2</sub> diss.			Nozzle exit plane			Mode midpoint		
multiplier	mole/s	fract.	N	<i>T</i> , K	P, torr	M	T, K	P, torr	M
90	0.00	0.95	4.7	161	5.0	2.0	164	4.4	2.0
0	0.16	0.0	0.0	157	5.0	2.0	150	4.1	2.1
100	0.16	0.95	5.7	167	5.2	2.0	173	4.8	2.0

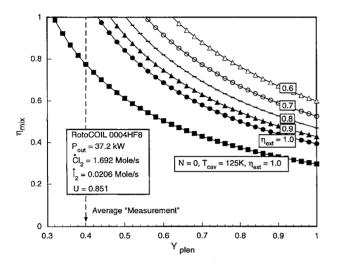


Fig. 5 Effect of  $\eta_{\rm ext}$  on heuristic constraint equation: N=6,  $T_{\rm cav}=170$  K, and  $\eta_{\rm geo}=0.98$ .

vapor present. For RotoCOIL, the temperature conditions in the generator and cold traps are such that the water partial pressure is on the order of 1-2 torr at the nozzle plenum. This corresponds to a molar flow rate of approximately 0.16 mole/s for test 0004HF8. Under such conditions, N increases as a result of water deactivation of  $I^*$  and excited  $I_2$  during the dissociation process. These code simulations indicate that N is increased to at least 5.7 including only the kinetic effects of water. The cavity temperature at the mode midpoint is predicted to increase from 150 K with no dissociation to 173 K including water and dissociation effects. The predicted cavity pressure at the mode midpoint of 4.8 torr compares very favorably with the measured cavity pressure from taps along the optical cavity wall of 4.7 torr, which substantiates the conclusion that  $T_{\rm cav}$  must be greater than the isentropic value of 125 K.

Figure 5 shows a series of constraint lines to show the sensitivity to  $\eta_{\rm ext}$ . The lowest is again the lowest line on Fig. 4. The next line up is for N=6,  $T_{\rm cav}=170$ , and  $\eta_{\rm ext}=1.0$ . The successive lines upwards are for  $\eta_{\rm ext}=0.9, 0.8, 0.7$ , and 0.6. The separation of the lowest and next lowest lines represents the estimate of the combined loss as a result of  $Y_{\rm diss}$ , dissociation loss, and  $Y_{\rm th}$ , threshold yield, based upon code and experimental results. Also shown in Fig. 5 is the average measured value of  $Y_{\rm plen}$  for this test. Clearly it is outside the boundary of any constraint line, especially in view of the fact that  $\eta_{\rm ext}$ , as will be discussed later, is significantly less than 1. This is why  $Y_{\rm plen}$  is being treated as an unknown, as discussed earlier.

At this point the actual combination of the remaining unknowns  $\eta_{\rm mix}$ ,  $Y_{\rm plen}$ , and  $\eta_{\rm ext}$  must lie somewhere in the region of Fig. 5 that is above and to the right of the constraint line labeled  $\eta_{\rm ext}=1$ . However,  $Y_{\rm plen}$  must be substantially less than 1 because there is substantial ducting between the generator and the nozzle and the yield parameter at the generator cannot be greater than 1. In the next section the loss during generation and ducting to the nozzle will be evaluated. Following that,  $\eta_{\rm ext}$  will be evaluated.

# **Generation and Transport**

To estimate the generation and transport losses of  $O_2(^1\Delta)$  from the RotoCOIL rotating disk generator and delivery system, the DEOX code developed by Crowell<sup>13</sup> was used. This code couples

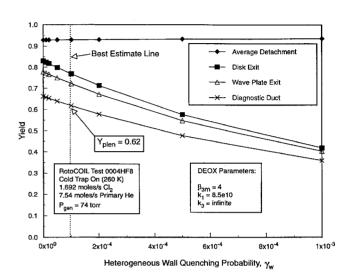


Fig. 6 Effect of heterogeneous wall quenching probability  $\gamma_{\rm w}$  on RotoCOIL generator/delivery yield profile.

a two-dimensional wetted wall reactor model to a one-dimensional aerokinetic transport model to describe the evolution of  $O_2(^1\Delta)$ (hence  $Y_{plen}$ ) for the RotoCOIL generator and delivery system. Reference 14, which presents an analytic solution to this problem, gives a comprehensive review of the COIL generator/delivery modeling approach, associated set of rates, and other modeling parameters that are used in the DEOX code and a critique regarding how well these parameters are known. The DEOX model, which gives a numerical solution to the same governing partial differential equations, is used in the present study to remove the uncertainties associated with the approximations used to develop the analytic result of Ref. 14. As discussed in Ref. 14, not all of the relevant rate constants are known. The uncertainties associated with chlorine utilization were eliminated in the present analysis by setting the parameters that affect this process so that the code results match the measured utilization of 0.85 in test 0004HF8. Two parameters in DEOX directly affecting the production of  $O_2(^1\Delta)$  that are largely unknown are the  $O_2(^1\Delta)$  production rate  $k_3$  and the heterogeneous deactivation rate  $\gamma_w$  for  $O_2(^1\Delta)$  on the liquid basic hydrogen peroxide surface in the generator. To obtain an upper bound of  $Y_{plen}$ ,  $k_3$  was set to infinity and a set of DEOX calculations were made varying  $\gamma_m$ . Predictions of yield at various locations through the generator/delivery system are presented in Fig. 6, including at the BHP liquid surface (detachment yield), at the disk exit, and at the Roto-COIL diagnostic duct where yield measurements were made. Using  $k_3 = \infty$  and  $\gamma_w = 0$  gives from Fig. 6 the highest upper bound for  $Y_{\text{plen}}$  of 0.66. In general, the data do not support a value for  $\gamma_w$  of zero. An estimate of  $5 \times 10^{-5}$  is suggested by Ref. 15 for ducting. A higher value is expected on BHP-coated surfaces. For purposes of a more reasonable upper bound than 0.66, a value of  $1 \times 10^{-4}$  is selected here. This gives from Fig. 6 a best estimate upper bound of 0.62. Both the absolute and best estimate upper bound for  $Y_{plen}$  are plotted on the constraint curve in Fig. 7. The shaded area in Fig. 7 represents the constraints on parameters from arguments presented thus far.

# **Extraction Efficiency**

To evaluate extraction efficiency  $\eta_{\rm ext}$  and to determine the dependence of the extraction efficiency on the mixing efficiency  $\eta_{\rm mix}$ , a heuristic expression for extraction efficiency was utilized. It is based

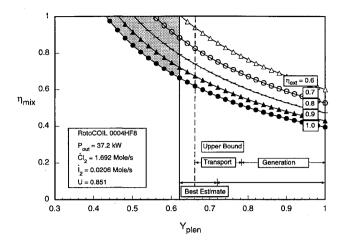


Fig. 7 Effect of  $Y_{\rm plen}$  bounding analysis on heuristic solution space (defined by light gray area): N=6,  $T_{\rm cav}=170$  K, and  $\eta_{\rm geo}=0.98$ .

on the assumption that a COIL device responds to photon flux like a Rigrod laser. This is not strictly true because, in Rigrod lasers, the gain species is the same as the energy containing species, and so power is extracted directly as the gain saturates. In a COIL device, however, because energy transfers from the  $O_2(^1\Delta)$  to the iodine lasing species, the power is extracted indirectly with gain saturation. Nevertheless, as will be seen from experimental data, the saturation characteristics of RotoCOIL are described quite closely by a Rigrod-like saturation curve. The COIL extraction efficiency is expected to be somewhat higher than that determined by a Rigrod-type analysis for reasons to be described.

The heuristic power extraction efficiency is developed as a product of the basic Rigrod extraction efficiency  $\eta_{\rm extr}$ , times the extraction efficiency of the resonator  $\eta_{\rm extr}$ . Thus the outcoupled power is given by

$$P_{\rm out} = P_{\rm av} \eta_{\rm ext} \tag{21}$$

where

$$\eta_{\rm ext} = \eta_{\rm extm} \eta_{\rm extr} \tag{22}$$

and

$$\eta_{\text{extm}} = 1 - G_{\text{th}}/G_{\theta} \tag{23}$$

Because all of the power that is extracted from the gain medium is not in the output beam

$$\eta_{\text{extr}} = \frac{P_{\text{out}}}{P_{\text{out}} + \text{ all other losses}}$$
 (24)

In the preceding,  $G_{\rm th}$  is the threshold gain of the resonator:

$$G_{\rm th} = \frac{-\ln(R_{\rm out}R_{\rm max})}{2L_g} \tag{25}$$

The other losses in Eq. (25) include the mirror scattering and absorption losses, the power out of  $R_{\rm max}$ , and diffraction losses. In this analysis, the mirror reflectivities and scattering coefficients are treated as measured quantities, but because the diffraction losses were not measured, an analytic estimate made in Appendix A of Ref. 16 is used. A nonsaturable distributed loss is not considered in the gain region in this analysis because the estimated diffraction and mirror scattering losses are seen to be sufficient to explain the measured power saturation data for RotoCOIL.

Treating the diffraction loss as a fraction  $\mathcal{P}$  of the outcoupled power,  $\eta_{\text{extr}}$  is given by

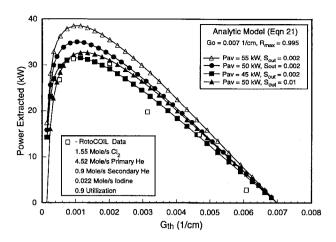


Fig. 8  $-\eta_{ext}$  determined from heuristic extraction efficiency analysis of RotoCOIL power saturation data.

The two  $S_{\rm max}$  terms are retained for illustrative purposes. The factor  $(R_{\rm out}/R_{\rm max})^{1/2}$  accounts for the fact that the flux at  $R_{\rm max}$  is somewhat less than at  $R_{\rm out}$  and the factor  $A_{\rm max}/A_{\rm out}$  accounts for the larger beam footprint at  $R_{\rm max}$  because the resonator is half symmetric. For the present resonator configuration,  $A_{\rm max}/A_{\rm out}$  is estimated to be 1.06. The terms  $S_{\rm out}$  and  $S_{\rm max}$  are the scattering coefficients at  $R_{\rm out}$  and  $R_{\rm max}$ , respectively, and can include absorption loss if comparable.

To develop a bounding estimate of  $\eta_{\text{ext}}$ , the heuristic extraction efficiency model is compared with available RotoCOIL saturation data. Figure 8 presents experimental power saturation data as a function of threshold gain for a series of RotoCOIL tests with the  $R_{\text{out}}$  mirror varied<sup>5</sup> as well as a series of analytic predictions from Eq. (21). These data are for average flow conditions as given on the figure that were very similar, but not identical, to test 0004HF8. The parameters that need to be specified in Eq. (21) to generate a power prediction include  $P_{av}$ ,  $G_o$ ,  $R_{out}$ ,  $S_{out}$ , and P. An average  $G_o$ of 0.007 cm<sup>-1</sup> was determined by visually extrapolating the experimental saturation data of Fig. 8 to the zero power location on the threshold gain axis. Lasing ceases at this point because threshold gain has increased to  $G_o$ . Using the analytically derived diffractive loss  $\mathcal{P}$  variation with  $R_{\text{out}}$  from Ref. 16 leaves  $P_{\text{av}}$ ,  $R_{\text{out}}$ , and  $S_{\text{out}}$ to be specified. From scattering and reflectivity measurements conducted on similar optics to test 0004HF8, it is believed that  $R_{\rm out}$ and  $S_{\rm out}$  can be no better than 0.995 and 0.002, respectively. The bounding analysis consists of successively varying  $P_{\rm av}$  and  $S_{\rm out}$  to just match the experimental saturation curve with the results given in Fig. 8. The top three curves (open triangle, solid circle, and solid square) show the effect of successive reductions in  $P_{av}$  from 55 to 45 kW with  $S_{\rm out}$  fixed at 0.002. The peak extraction efficiency for each of these curves is 0.7. The 50-kW prediction is seen to fully encompass the full set of experimental data, thus providing an upper bound on  $\eta_{\rm ext}$ . Reducing  $P_{\rm av}$  to 45 kW causes the prediction to match the peak experimental data point, but the rolloff in the prediction with lower threshold gain is underpredicted, indicating there are higher resonator losses in the experimental data compared with the prediction. By increasing the resonator loss for  $P_{\rm av}=50~{\rm kW}$  to  $S_{\rm out} = 0.01$ , a very good match with the experimental data is made both in terms of magnitude and profile. The predicted extraction efficiency for this case dropped to 0.65.

An adjustment must now be made to this bounding estimate for  $\eta_{\rm ext} = 0.70$  to account for the differences between COIL and Rigrod saturation characteristics. A reasonable assumption is made that the difference between the two estimates resides in the medium extraction term only. Manipulating the simplified saturation model derived by Crowell and Plummer, <sup>14</sup> one can show that the medium

$$\eta_{\text{extr}} = \frac{(1 - R_{\text{out}} - S_{\text{out}})}{(1 - R_{\text{out}} - S_{\text{out}})(1 + \mathcal{P}) + S_{\text{out}} + (R_{\text{out}}/R_{\text{max}})^{\frac{1}{2}} (A_{\text{max}}/A_{\text{out}})(1 - R_{\text{max}} - S_{\text{max}} + S_{\text{max}})}$$
(26)

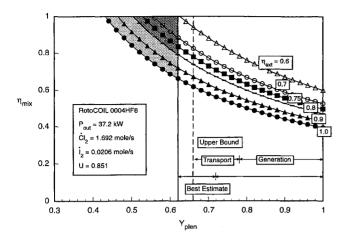


Fig. 9 Effect of  $\eta_{\rm ext}$  bounding analysis on reducing the heuristic solution space (identified by dark gray area): N=6,  $T_{\rm cav}=170$  K, and  $\eta_{\rm geo}=0.98$ .

extraction efficiency for COIL  $(\eta_{\text{extm}})_{\text{COIL}}$  is simply the product of the Rigrod medium extraction efficiency  $(\eta_{\text{extm}})_{\text{Rigrod}}$  and the factor

$$(\eta_{\text{extm}})_{\text{COIL}} = (\eta_{\text{extm}})_{\text{Rigrod}} \left[ \frac{1}{1 - \phi G_{\text{th}} / G_{o}} \right]$$
 (27)

where  $\phi$  is a COIL chemistry parameter that varies between 0 and 1 and is given as a function of  $Y_{\rm cav}$ , which is  $Y_{\rm plen}-Y_{\rm diss}$ ,  $Y_{\rm th}$ , and  $k_{\rm ca}$  by

$$\phi = \frac{(k_{\rm eq} - 1)(Y_{\rm cav} - Y_{\rm th})}{1 + Y_{\rm cav}k_{\rm eq} - Y_{\rm cav}}$$
(28)

Taking into account the range of uncertainty in  $Y_{\rm cav}$  and  $T_{\rm cav}$  for test 0004HF8,  $\phi$  is bounded between 0.55 and 0.75. Using  $\phi=0.65$  as the average of this uncertainty range together with an assumed 20% increase in  $G_o$  to account for test 0004HF8 flow differences from those for Fig. 8 gives the multiplying factor as 1.138, which provides the upper bound estimate for  $(\eta_{\rm ext})_{\rm COIL}$  equal to 0.80. This value is plotted on Fig. 9 and closes in the bounding triangle for parameter space for test 0004HF8.

# Dependence of $\eta_{\mathrm{ext}}$ on $\eta_{\mathrm{mix}}$

The form of the heuristic equation basically assumes that  $\eta_{\rm ext}$  does not depend upon  $\eta_{\rm mix}$ . This is not quite true, but it will be shown here that for the values of  $\eta_{\rm mix}$  that fit into the parameter space for test 0004HF8 this is a very good approximation. When  $\eta_{\rm mix}$  is less than unity, the potential effect on extraction efficiency is through the effect of gain dependence on two factors,  $Y_{\rm cav}$  and  $T_{\rm cav}$ . First, the dependence of gain on  $Y_{\rm cav}$ , the  $O_2({}^1\Delta)$  yield in the laser cavity, and  $T_{\rm cav}$  is determined starting from the definition of gain given by

$$G_o = \sigma (293/T_{\text{cav}})^{\frac{1}{2}} ([I^*] - \frac{1}{2}[I])$$
 (29)

As noted earlier, there is an equilibrium between  $I^*$ ,  $O_2(^1\Delta)$ , and  $O_2(^3\Sigma)$  given by

$$\frac{[I^*]}{[I]} = \frac{k_{eq}[O_2(^1\Delta)]}{O_2(^3\Sigma)}$$
(30)

Combining Eq. (29) with Eq. (30) gives, after some algebra,

$$G_o = \sigma \left(\frac{293}{T_{\text{cav}}}\right)^{\frac{1}{2}} [I_2] F \left[\frac{(1+2k_{\text{eq}})Y_{\text{cav}} - 1}{(k_{\text{eq}} - 1)Y_{\text{cav}} + 1}\right]$$
(31)

where

$$Y_{\text{cav}} = Y_{\text{plen}} - \frac{N\dot{1}_2 F}{\dot{C}l_2 U_{\text{Cl}_2} \eta_{\text{mix}}}$$
 (32)

where  $\sigma$  is equal to 7.5  $\times$  10<sup>-18</sup> cm<sup>2</sup> and [I<sub>2</sub>] is the I<sub>2</sub> density per cubic centimeter. When  $\eta_{mix}$  does not equal unity, the effective I<sub>2</sub> density is [I<sub>2</sub>]/ $\eta_{mix}$ .

However, the region in the nozzle flow that has gain is reduced by  $\eta_{\text{mix}}$ . Thus the average  $G_o$  in one nozzle flow is made up of two gain regions, one that is  $\eta_{\text{mix}}d$  wide having a gain  $(G_o)_{\eta_{\text{mix}}}$ , where d is the nozzle exit width, and a region  $d(1-\eta_{\text{mix}})$  where there is no  $I_2$  and therefore no gain. From this the average  $G_o$  is given across each nozzle and therefore across the entire gain length as

$$\bar{G}_o = \frac{\eta_{\text{mix}} d(G_o)_{\eta_{\text{mix}}} + d(1 - \eta_{\text{mix}})(0)}{d} = (G_o)_{\eta_{\text{mix}}} \eta_{\text{mix}}$$
(33)

Because  $(G_o)_{\eta_{\rm mix}}$  is just  $G_o$  from Eq. (31) divided by  $\eta_{\rm mix}$  (because  $[{\rm I_2}]$  is replaced by  $[{\rm I_2}]/\eta_{\rm mix}$ ) in this simple two-zone model, the average  $G_o$  is the  $G_o$  given by Eq. (31), with  $Y_{\rm cav}$  given by Eq. (32) but with  $T_{\rm cav}$  as determined next.

When  $\eta_{\rm mix}$  is less than 1, the heat of dissociation is delivered to less of the flow. This increases the temperature in this portion of the flow compared with the fully mixed situation. Thus  $T_{\rm cav}$  in this region is higher. Because this is the region where there is gain, the  $T_{\rm cav}$  in Eq. (30) is higher, depending on  $\eta_{\rm mix}$ . Aerodynamic code analysis (Table 3) shows that the heat of dissociation increases  $T_{\rm cav}$  when fully mixed, from 150 to 173 K for N=5.7. Therefore  $T_{\rm cav}$  in the gain equation is scaled by  $T_{\rm cav}=150\,{\rm K}+23/\eta_{\rm mix}$ .

From the preceding,  $G_o$  and therefore  $\eta_{\rm extm}$  and  $\eta_{\rm ext}$  depend on  $\eta_{\rm mix}$  through  $Y_{\rm diss}$  and  $T_{\rm cav}$ . Figure 10 shows the dependence of  $G_o$ , the dependence of  $\eta_{\rm extm}$  (the higher curve), and the dependence of the overall  $\eta_{\rm ext}$  (the lower curve) on  $\eta_{\rm mix}$ , which includes the resonator extraction efficiency for RotoCOIL with  $R_{\rm out}=0.85$ . As can be seen, for  $\eta_{\rm mix}$  greater than 0.5,  $\eta_{\rm ext}$  is essentially constant; thus assuming  $\eta_{\rm ext}$  to be independent of  $\eta_{\rm mix}$  is legitimate in the heuristic equation for values of  $\eta_{\rm mix}$  that are in the parameter space for test 0004HF8.

#### Results

Based on the preceding analysis and discussion, the partition of the losses in test 0004HF8 is summarized in Table 4 for a point at the center of the solution space given in Fig. 9 (dark triangle). The results in Table 4 can be distributed to the major components,

Table 4 Chemical efficiency loss accounting for RotoCOIL test 0004HF8 using midpoint of heuristic solution space

Location	Loss parameter	Normalized power in flow
Generator entrance		1.0
BHP film interface	$U_{\text{Cl}_2} = 0.851$	0.851
	$Y_{\text{detach}} = 0.90$	0.766
Generator exit	$Y_{\text{exit}} = 0.74$	0.630
Delivery	$Y_{\rm plen} = 0.59$	0.502
Nozzle	$Y_{\rm diss} = 0.086$	0.429
	$Y_{\rm th} = 0.059$	0.379
	$\eta_{\rm mix} = 0.94$	0.356
Resonator	$\eta_{\rm geo} = 0.98$	0.349
	$\eta_{\rm ext} = 0.70$	0.244
$\eta_{ m chem}$	·	0.244

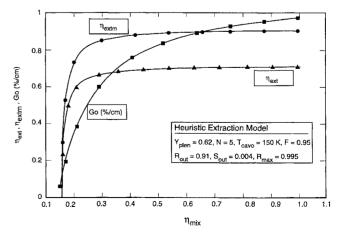


Fig. 10 Effect of  $\eta_{\rm mix}$  on  $\eta_{\rm ext}$  from the heuristic extraction efficiency model.

Table 5 Distribution of losses by major COIL device components

Device component	Percentage loss	Comment
Generator	37.0	Includes internal transport loss but no water losses
Delivery	12.8	
Nozzle	14.6	Includes water loss (1.5% for increased $N$ and 2.7% for increased $T_{cav}$ ) but no gain effects
Resonator	11.2	Includes $\eta_{geo}$
Power out	24.4	

as shown in Table 5. Note that the results in Table 4 are based on a detachment yield of 0.90. This value is in agreement with other experimental data.17

Clearly the largest contributor to losses is the combination of generation and transport losses, which represent over half of the total loss. The rest of the losses are about half and half between nozzle and extraction. Some of the losses, i.e., the minimum dissociation loss (N = 2 compared with 0) and  $Y_{th}$  for  $T_{cav}$  up to 125 K, are unavoidable consequences of the physics of the laser.

#### IV. Summary and Conclusions

A number of conclusions can be drawn regarding the nature of the losses (reduction in overall chemical efficiency) in the RotoCOIL device. Some of the observations, particularly for the oxygen generator, are sufficiently general that they apply to any type of oxygen generator that is based on the reaction of gaseous chlorine with liquid basic hydrogen peroxide and, therefore, indicate the direction to be taken to improve device performance.

#### RotoCOIL

From the values summarized in Table 5, the oxygen generator (including wave plate separator) is the RotoCOIL component with the highest loss (37.0%). Note that the chemistry loss is 23.4% ( $U_{Cl_2}$  = 0.851 and  $O_2(^1\Delta)$  detachment yield is 0.90), whereas the internal transport loss is 15.6%. The nozzle mixing and resonator losses are comparable, 14.6 and 11.2%, respectively. The ducting loss is moderate, in comparison, 12.8%, but when the generator internal transport loss is added to the ducting loss, transport losses, 28.4%, are the largest single contribution to loss in the RotoCOIL device.

The average of the measured values of  $O_2(^1\Delta)$  during the RotoCOIL test 0004HF8 was too low to be correct. Figure 5 shows that the average value just does not fit into the parameter space. This was true of other RotoCOIL tests as well. Nominal experimental error bars of  $\pm 20\%$  would still leave the measurement out of the parameter space, despite the fact that the diagnostic instrumentation was carefully calibrated. This discrepancy is unexplained.

The nozzle injection and mixing losses in RotoCOIL are deduced to be modest, not the primary source of loss. Also, the RotoCOIL power extraction efficiency is in line with expectations for a device of this gain length, 54 cm, given the mirror scatter and diffraction losses.

#### **General Conclusions**

Based on the RotoCOIL evaluation, there are some conclusions that are more general and would apply to other devices. This evaluation indicates that at the RotoCOIL generator flow and pressure regime of about 75 torr, the generator chemistry is rather effective, namely, detachment yield of about 90% and utilization of 85%. The detachment yield deduced here is in agreement with other experimental data. Furthermore, these experiments have shown that increasing the disk pack rotation rate above 20 rpm (the RotoCOIL nominal) to 30-40 rpm increases utilization above 90% with no detrimental effect on yield. Thus, the basic physics and chemistry of the reaction of chlorine with basic peroxide are quite effective in producing  $O_2(^1\Delta)$  in large quantities. The mixing of  $I_2$  into the subsonic entry plenum of a supersonic nozzle also is quite effective in this flow and pressure regime. It is suggested that although mixing is not perfect, there is not a lot of room for improvement.

#### **Future Directions**

These results also indicate the direction that further efforts to improve COIL performance need to take for the major elements of a COIL device.

#### Generator

Generally higher-pressure operation will result in a reduced impact of water vapor because it will reduce its molar fraction in the flow. Also, increased pressure will make generators smaller, which is required to minimize ducting losses while feeding nozzles at higher pressure. There will be benefits realized from generator concepts where the surface film temperature is colder to further reduce the impact of water vapor. Care must be taken to not reduce  $O_2(^1\Delta)$  and  $U_{\text{Cl}_2}$  in the process. Also, increasing the ratio of BHP flow/Cl<sub>2</sub> flow would be beneficial in maintaining fresher BHP to the Cl<sub>2</sub> flow, thus elevating  $U_{\text{Cl}_2}$  and possibly  $O_2(^1\Delta)$  yield simultaneously. Clearly, the internal volume of generators must be made smaller to reduce internal transport losses.

#### Ducting

Along with volume reduction within the generator, care must be taken to design only the absolute minimum of ducting from the generator to the nozzle. This becomes even more important at highpressure operation. In other words, get the nozzle as close to the generator as physically possible.

#### Nozzle/Mixing

As generators are improved by working at higher pressures, nozzle design must follow suit. Injection hole size, patterns, and distance from the throat need to be optimized for higher flow and pressures. The I<sub>2</sub> dissociation processes and rate constants need to be affirmed to aid in analyzing changes required by higher-pressure operation. Also, as devices become larger, i.e., gain length becomes longer, greater care in designing the supersonic expansion contours of the nozzle, the optical cavity, and the nozzle/cavity interface to minimize cavity pressure (density) variations will be required.

# Resonator/Power Extraction

Generally larger devices will lead to reduction of extraction losses. Taller nozzles will increase  $\eta_{geo}$ . With longer gain length, extraction efficiency will be increased, possibly sufficient to permit lower I<sub>2</sub> flows. This would reduce dissociation losses, which in turn would result in somewhat lower cavity temperatures because of reduced heat added to the flow by dissociation. Lower cavity temperatures would reduce the  $Y_{th}$  loss. These would be relatively small effects individually but in concert could be significant, especially with reduced impact of water vapor, which is very detrimental to performance, when operating at higher generator pressure.

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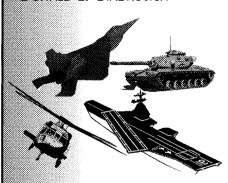
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# **Operations Research Analysis in Test and Evaluation**

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The publication of this text represents a significant contribution to the available technical literature on military and commercial test and evaluation. Chapter One provides important history and addresses the vital relationship of quality T&E to the acquisition and operations of defense weapons systems. Subsequent chapters cover such concepts as cost and operational effectiveness analysis (COEA), modeling and simulation (M&S), and verification, validation, and accreditation (VV&A), among others. In the closing chapters, new and unique concepts for the future are discussed.

The text is recommended for a wide range of managers and officials in both defense and commercial industry as well as those senior-level and graduate-level students interested in applied operations research analysis and T&E.

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